

Problem Solution #7

Problem 1

$$V = V_0 \sin \omega t = 120\sqrt{2} \sin(2\pi \times 60t)$$

$$B = B_0 \cos \omega t = 1.8 \cos(2\pi \times 60t)$$

$$V = -N \frac{d\Phi}{dt} = -N \frac{dB}{dt} S = NSB_0 \omega \sin \omega t$$

$$\text{So } N = \frac{120\sqrt{2}}{6 \times 10^{-4} \times 1.8 \times 2\pi \times 60} \approx 417 (\text{turns})$$

Problem 2

$$\vec{E} = \frac{Q}{2\pi\epsilon r} \hat{r} \quad V = \frac{Q}{2\pi\epsilon} \ln\left(\frac{b}{a}\right),$$

$$\text{So } E = \frac{V}{r \ln(b/a)} = \frac{100 \cos(12\pi \times 10^6 t)}{r \ln(4/2)}$$

$$\vec{D} = \epsilon \vec{E} = \epsilon_0 \epsilon_r \vec{E}$$

$$I_d = \frac{d\vec{D}}{dt} \cdot \vec{A} = 8.85 \times 10^{-12} \times 3.7 \times \frac{-100 \times 12\pi \times 10^6 \sin(12\pi \times 10^6 t)}{r \ln(4/2)} \hat{r} \cdot 2\pi r \hat{r}$$

$$= 2\pi \times 8.85 \times 10^{-12} \times 3.7 \times \frac{-100 \times 12\pi \times 10^6 \sin(12\pi \times 10^6 t)}{\ln(4/2)} \approx -1119 \sin(12\pi \times 10^6 t) \text{ mA}$$

$$I_c = I_d \Rightarrow \frac{\sigma}{\omega\epsilon} = 1 \Rightarrow \sigma \approx 1.23 \times 10^{-3} (S/m)$$

Problem 3

Lossless Medium:

$$\beta = \omega \sqrt{\mu\epsilon} = 2\pi f \sqrt{\mu_0 \epsilon_r \epsilon_0} \approx 53.5 (\text{rad/m})$$

$$u = \omega / \beta = \frac{c}{\sqrt{\epsilon_r}} \approx 1.76 \times 10^8 (m/s)$$

$$\lambda = 2\pi / \beta \approx 0.117 (m)$$

$$\eta = \sqrt{\frac{\mu}{\epsilon}} \approx 221 (\Omega)$$

Problem 4

Linear polarization ($K > 0$, in-phase; $K < 0$, out-phase)