

**ENGR-4300**  
**Fall 2008**  
**Test 2**

**Name:** \_\_\_\_\_

**Section: 1(MR 8:00) 2(TF 2:00)**  
**(circle one)**

Question I (20 points): \_\_\_\_\_

Question II (20 points): \_\_\_\_\_

Question III (20 points): \_\_\_\_\_

Question IV (20 points): \_\_\_\_\_

Question V (20 points): \_\_\_\_\_

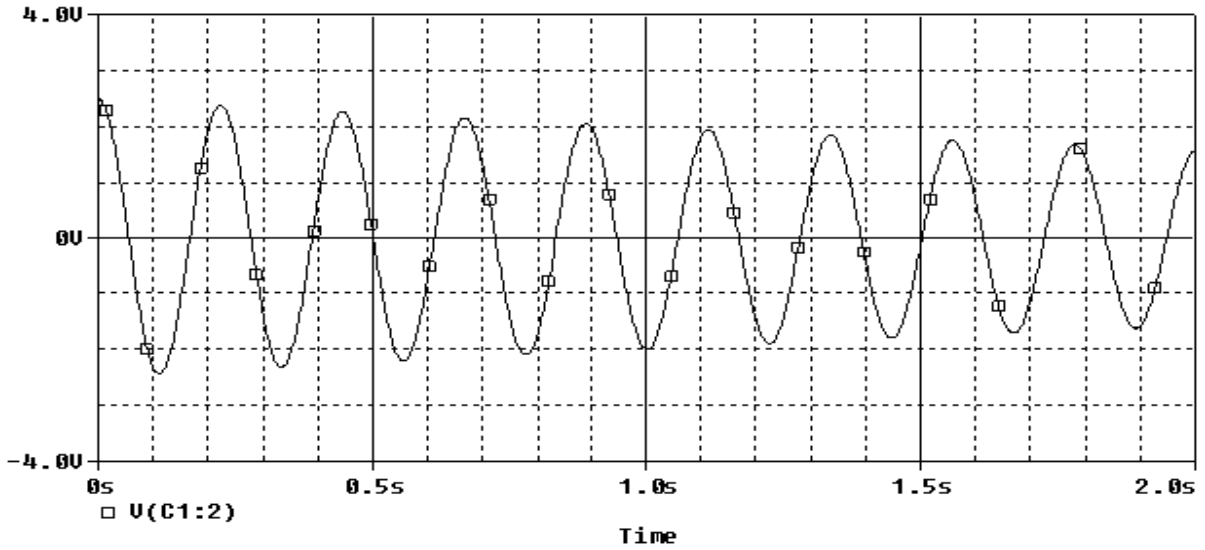
Total (100 points): \_\_\_\_\_

On all questions: SHOW ALL WORK. BEGIN WITH FORMULAS, THEN SUBSTITUTE VALUES AND UNITS. No credit will be given for numbers that appear without justification.

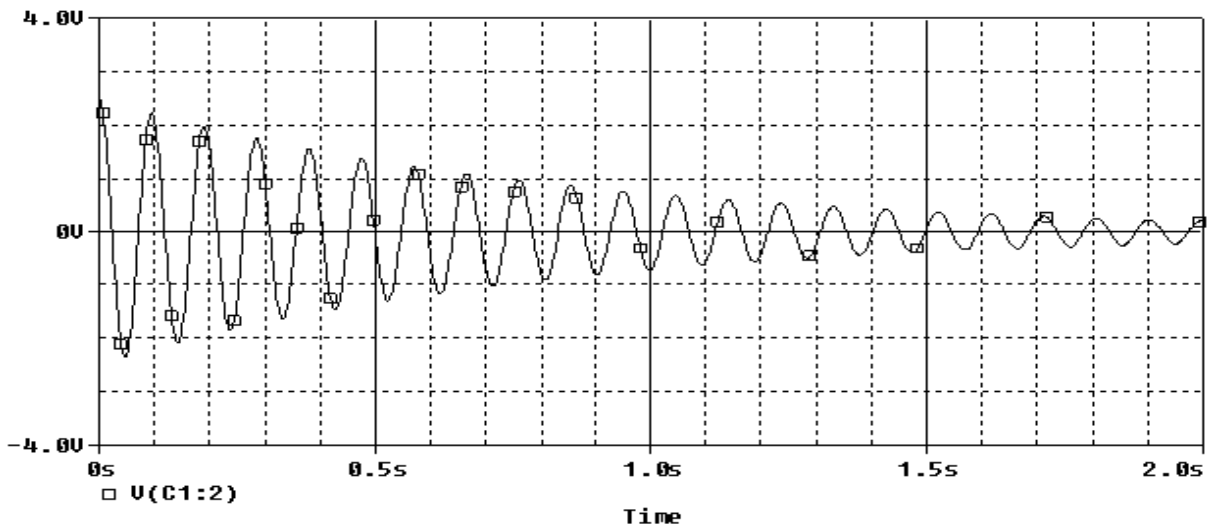
**Question I – Bridges and Damped Sinusoids (20 points)**

You are given a cantilever beam similar to the one you used in experiment 4. You place two weights on the end of the beam one at a time (0.1 kg and 0.7 kg) and you get the following two plots (may not be in order of mass listed).

**Plot 1**



**Plot 2**



1) (2pt) What is the frequency of plot 1? (Use at least 2 significant figures)

**Question I – Bridges and Damped Sinusoids (continued)**

2) (2pt) What is the frequency of plot 2? (Use at least 3 significant figures)

3) (6pt) What is the damping constant for plot 1, mark the points on the plot? (Use at least 3 significant figures)

4) (6pt) Given the following formula,  $k = (m + m_n) \cdot (2 \cdot \pi \cdot f_n)^2$ , and assuming that the two data points that you found are ideal, find values for k and m.

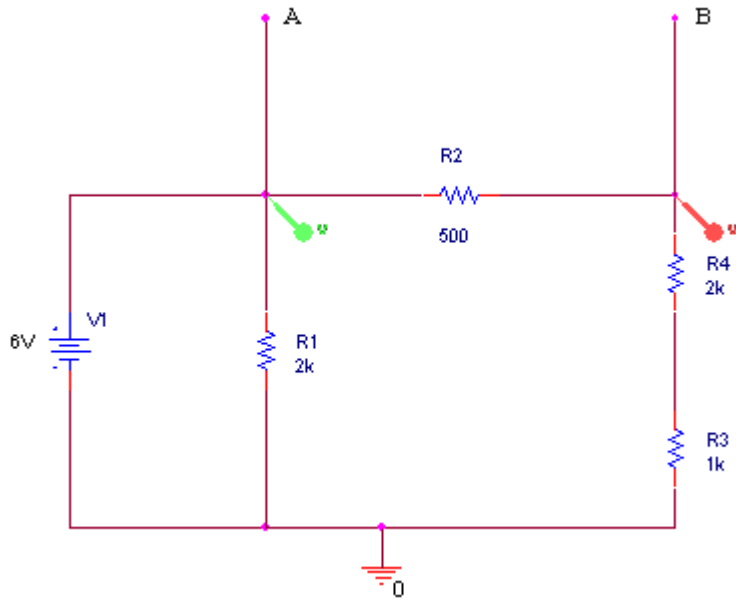
**Question I – Bridges and Damped Sinusoids (continued)**

5) (2pt) What is the mass of the beam?

6) (2pt) Using the chart for Young's Modulus, determine the probable material that the beam is made out of given that the dimensions of the beam are: width = 1.5 cm, length=15 cm, and thickness = 2 mm.

TABLE 9.1			
Young's Modulus Table of Values			
Metal	Elastic modulus (N/m <sup>2</sup> )	Metal	Elastic modulus (N/m <sup>2</sup> )
aluminum, 99.3%, rolled	$6.96 \times 10^{10}$	lead, rolled	$1.57 \times 10^{10}$
brass	$9.02 \times 10^{10}$	platinum, pure, drawn	$16.7 \times 10^{10}$
copper, wire, hard drawn	$11.6 \times 10^{10}$	silver, hard drawn	$7.75 \times 10^{10}$
gold, pure, hard drawn	$7.85 \times 10^{10}$	steel, 0.38% C, annealed	$20.0 \times 10^{10}$
iron, wrought	$19.3 \times 10^{10}$	tungsten, drawn	$35.5 \times 10^{10}$

## Question II – Thevenin Equivalents (20 points)



- 1) (7pt) Find the Thevenin equivalent voltage with respect to A and B for the circuit shown above)  
*Hint:  $V_{th} = V_A - V_B$  so find  $V_A$  then  $V_B$*

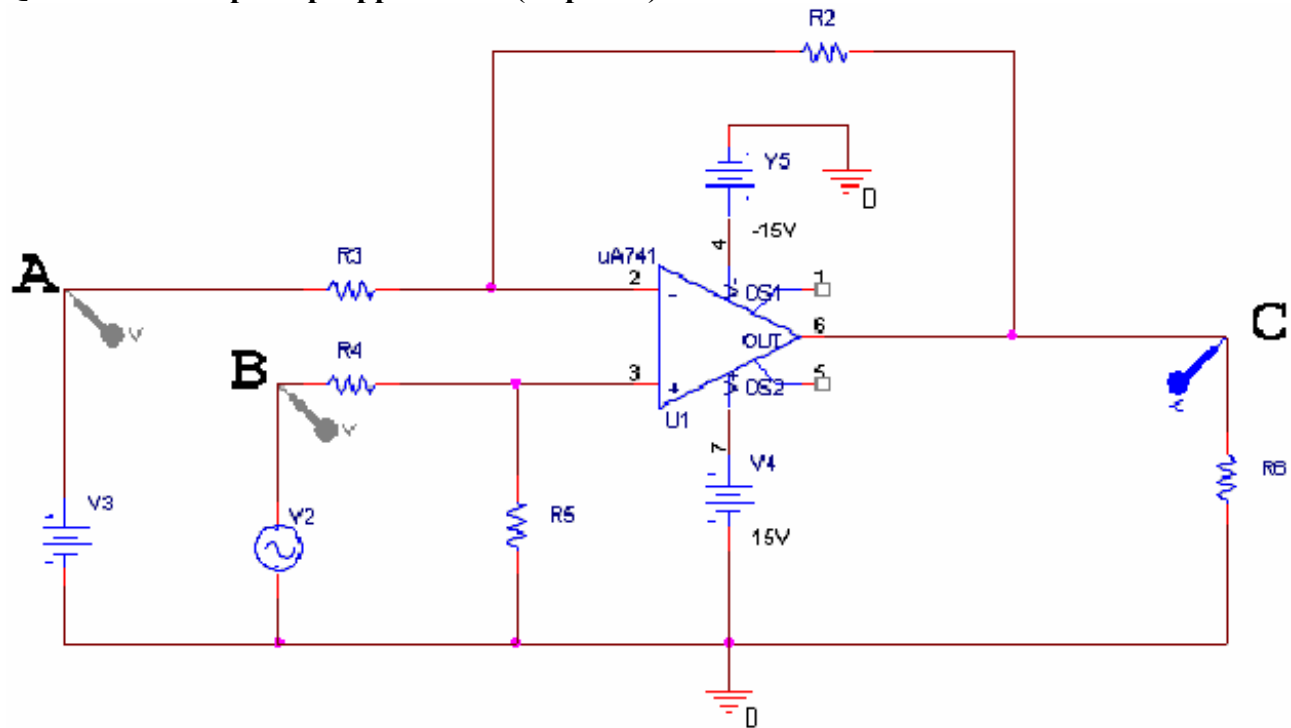
**Question II – Thevenin Equivalent (continued)**

2) (6pt) Find the Thevenin equivalent resistance with respect to A and B for the circuit shown above.

3) (5pt) Draw the Thevenin equivalent circuit with a load resistor  $R_L$  of 3K between points A and B

4) (2pt) What is the voltage across  $R_L$ ? *Hint: Also the voltage at point  $V_A$*

## Question III – Op-Amp Applications (20 points)



Assume the following components in the above circuit:

$$V_2 : V_{off}=2V, V_{amp}=2V, Freq=1k$$

$$V_3 : V_{dc}=2V$$

$$R_2 := 16k\Omega \quad R_3 := 2k\Omega \quad R_4 := 2k\Omega$$

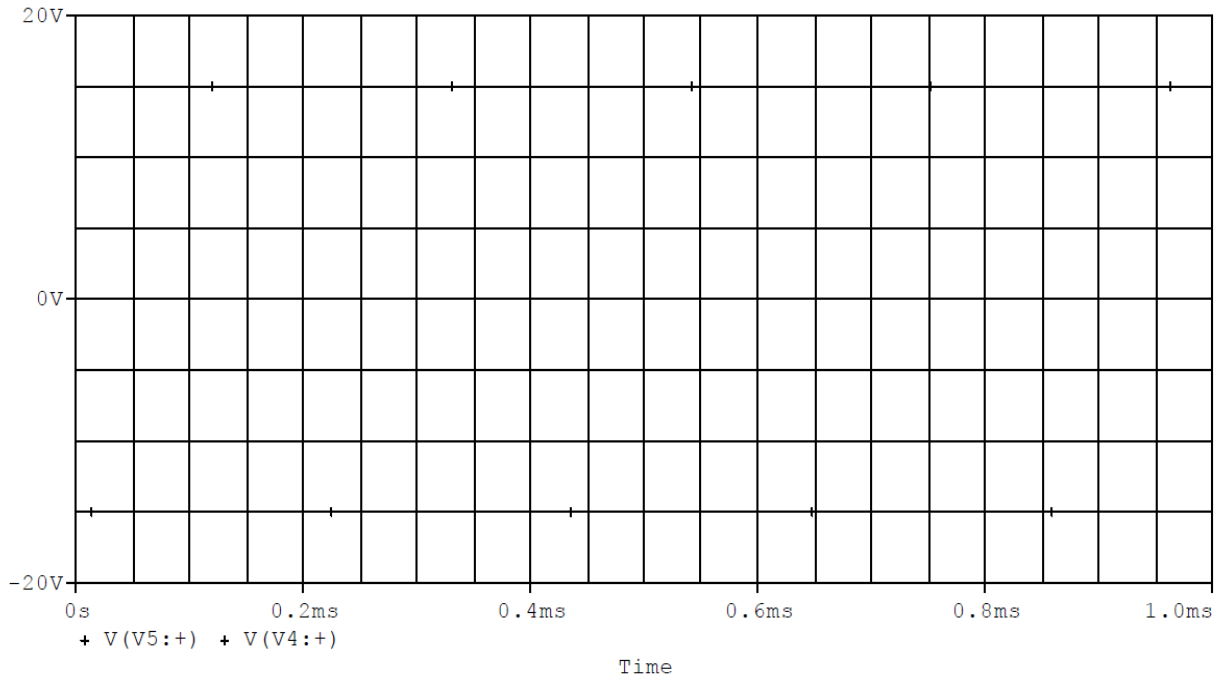
$$R_5 := 16k\Omega \quad R_6 := 1k\Omega$$

1) (1pt) The circuit above is an amplifier you've seen. What type of amplifier is it?

2) (3pt) Write an equation for the output C ( $V_c$ ) in terms of the input voltages  $V_2$  and  $V_3$ . Simplify (Do not have to enter voltage values)

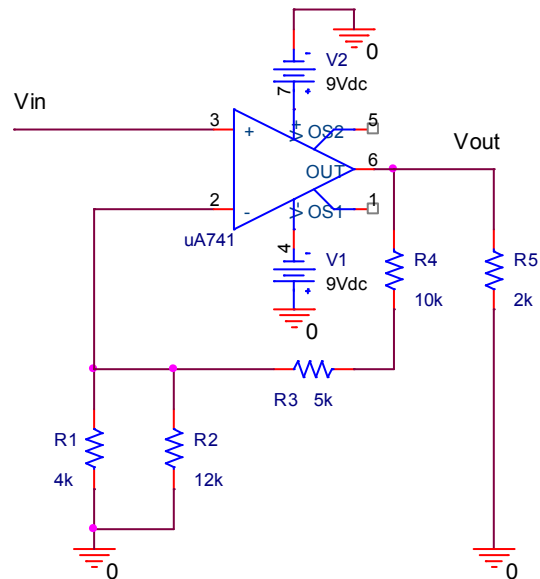
**Question III – Op-Amp Applications (continued)**

3) (16pt) Sketch and label one cycle of the input at V2 (point B), the input at V3 (point A) and the output at C (Vc) on the plot below





## Question IV – Op-Amp Analysis (20 points)



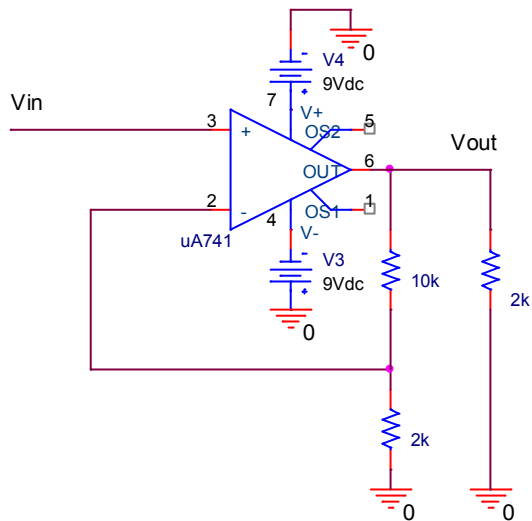
1) (2pt) What op-amp circuit given on your crib sheet does this circuit most closely represent?  
 a. Inverting Amplifier   b. Non-inverting Amplifier   c. Adder   d. Differential Amplifier  
 e. Practical Active Differentiator

2) (2pt) Redraw the circuit combining and resistors that are in parallel or series and find the combined values.

3) (2pt) What are the two golden rules of op-amp analysis?

## Question IV – Op-Amp Analysis (continued)

4) (2pt) Using a different circuit below, if  $V_{in} = 1V$  on the '+' input of the op-amp, what is the voltage on the '-' input?



5) (3pt) From 4), how much current is flowing through the  $2k$  resistor to ground?

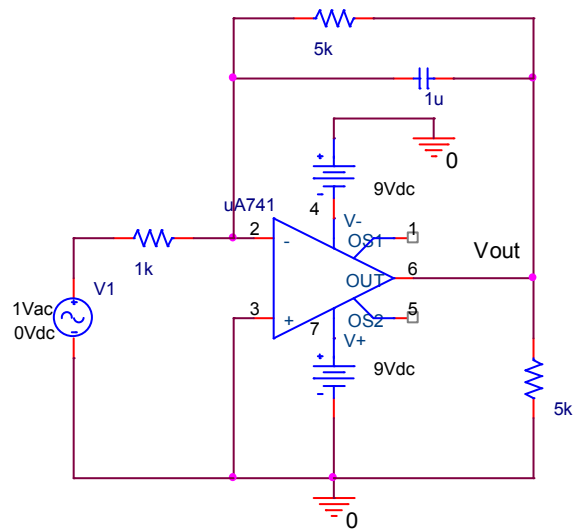
6) (3pt) By the Golden Rules, how much current in 4) is flowing through the  $10k$  resistor from  $V_{out}$  to  $V^-$  (the connection point between the 2 resistors)?

7) (3pt) What is  $V_{out}$  for  $V_{in} = 1V$ ?

8) (2pt) What is the gain of this op-amp circuit?

9) (1pt) For an ideal op-amp in 4), what is the maximum value the input voltage  $V_{in}$  can have before the output will not be able to exhibit the full amplification from 8)?

## Question V – Op-Amp Integrators and Differentiators (20 points)



1) (2pt) What function is this circuit designed to perform?

2) (4pt) Write the transfer function  $V_{out}/V_1$  for this circuit. (Substitute in the values provided for the components.)

3) (3pt) For which frequencies will the circuit perform the desired function?

- a. Low frequencies below  $\omega_c$
- b. Only a mid band of frequencies around  $\omega_c$
- c. High frequencies above  $\omega_c$

4) (3pt) Find the corner frequency for the circuit in Hz.

**Question V – Op-Amp Integrators and Differentiators (continued)**

5) (2pt) Redraw the circuit with an appropriate substitution for the capacitor as  $f \rightarrow 0$  for when the input V1 has a very low frequency.

6) (4pt) Show that simplification of the transfer function from 2) for small  $\omega$  gives the same results as the analysis of the redrawn circuit in 5).

7) (2pt) Sketch the output of the original circuit in 1) to a square wave input on the axis below. Show the correct shape of the waveform but don't worry about the amplitude scaling.

