Name: $\qquad$

## Section: 1(MR 8:00) 2(TF 2:00) 3(MR 6:00) (circle one)

> Question I (20 points):
> Question II (20 points):
> Question III (17 points):
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$\qquad$
Question IV (20 points): $\qquad$
Question V (23 points): $\qquad$

Total (100 points): $\qquad$

On all questions: SHOW ALL WORK. BEGIN WITH FORMULAS, THEN SUBSTITUTE VALUES AND UNITS. No credit will be given for numbers that appear without justification.

Question I - Bridges and Damped Sinusoids (20 points)


1) (4 pts) Find the period and frequency of this signal. Include units.
2) ( 2 pts ) What is the value of the DC offset?
3) ( 4 pts ) Write the mathematical expression for this signal and its offset. In general, this is given by $\mathrm{X}=\mathrm{X}_{0}+\mathrm{X}_{1} \sin \left(\omega \mathrm{t}+\Phi_{0}\right)$ which accounts for its frequency, phase shift, and offset. (Phase shift with respect to $\mathrm{t}=0$ )

The circuit below gives the simulation output below.

4) (3 pts) Find the damping constant $\alpha$ for this data (use points labeled for you to three significant figures).
5) (4 pts) Write the mathematical expression for this data in the form of $v(t)=A \cos (\omega t) e^{-\alpha t}$
6) ( 3 pt ) If the resistor is completely removed from the circuit and replaced with a wire, what will happen to the frequency and amplitude of the simulated output? Why?

Question II - Thevenin Equivalents (20 points)


1) ( 6 pts ) Find the Thevenin voltage (Vth) of the circuit inside the rectangle.
2) ( 6 pts ) Find the Thevenin resistance.
3) (4 pts) Draw the Thevenin equivalent circuit with the load ( 1 K ohms).
4) (4 pts) For the following Thevenin equivalent circuit (not the one above) find the voltage between $A$ and $B$ with a load of $2 K$ ohms.


## Question III - Op-Amp Applications (17 points)



Assume that $\mathbf{\pm 9}$ Volt power supplies have been properly connected to all five $\mathrm{op}-\mathrm{amps}$ in the circuit above.

1) ( 5 pt ) The circuit has $5 \mathrm{op}-\mathrm{amps}$ labeled as U1 through U5. State what the op-amp circuit is for each. Choices are: 1. Follower/Buffer, 2. Inverting Amp, 3. Non-inverting Amp, 4. Differentiator, 5. Integrator, 6. Adding (Mixing) Amp, 7. Difference (Differential) Amp, 8. Miller Integrator, 9. Practical Differentiator.

U1 Circuit: $\qquad$ U2 Circuit: $\qquad$ U3 Circuit: $\qquad$
U4 Circuit: $\qquad$ U5 Circuit: $\qquad$
2) (4pt) Determine the values relative to ground, of $\operatorname{Va}(\mathrm{t}), \mathrm{Vb}(\mathrm{t}), \mathrm{Vc}(\mathrm{t})$ and $\mathrm{Vd}(\mathrm{t})$ as functions of $\operatorname{Vin}(\mathrm{t})$ with $\mathrm{R} 1=20 \mathrm{k}, \mathrm{R} 2=20 \mathrm{k}, \mathrm{R} 3=4 \mathrm{k}, \mathrm{R} 4=3 \mathrm{k}, \mathrm{R} 5=10 \mathrm{k}, \mathrm{R} 6=20 \mathrm{k}, \mathrm{R} 7=30 \mathrm{k}, \mathrm{R} 8=10 \mathrm{k}, \mathrm{R} 9=1 \mathrm{k}, \mathrm{C} 1=$ $100 \mu \mathrm{~F}$ and $\mathrm{C} 2=68 \mu \mathrm{~F}$.
a) Voltage at point $\mathrm{Va}(\mathrm{t})$ :
b) Voltage at point $\operatorname{Vb}(\mathrm{t})$ :
c) Voltage at point $\mathrm{Vc}(\mathrm{t})$ :
d) Voltage at point $\operatorname{Vd}(\mathrm{t})$ :
3) (3pt) Determine the output voltage, $\operatorname{Vout}(\mathrm{t})$, as a function of $\mathrm{Vb}(\mathrm{t}), \operatorname{Vc}(\mathrm{t})$ and $\operatorname{Vd}(\mathrm{t})$.
4) $(4 \mathrm{pt})$ Now find $\operatorname{Vout}(\mathrm{t})$ as a function of $\operatorname{Vin}(\mathrm{t})$.
5) (1pt) What is a practical use for a voltage follower/buffer op-amp?

## Question IV - Op-Amp Analysis (20 points)



Assume that $\mathbf{\pm 9}$ Volt power supplies have been properly connected to the op-amp in the circuit above.

1) ( 2 pt ) What op-amp circuit given on your crib sheet does this circuit most closely represent?
2) (3pt) What feedback connection is necessary before the golden rule concerning the voltages on the two input terminals can be applied?
3) (10pt) Using the two golden rules of op-amp analysis, derive an expression for Vout in terms of V2 and the appropriate resistor values, when V1 has been set to 0Volts. You must use Ohm's Law and current laws to describe how the op-amp functions by the golden rules.
4) (4pt) Remove R4, set V2 = V1 (short the 2 inputs together), and derive the expression for Vout in terms of V1 and the resistors using the rules for op-amp analysis.
5) (1pt) What does R4 model or represent in this circuit?

## Question V - Op-Amp Integrators and Differentiators (23 points)

In the circuit below, $\mathrm{Rin}=200 \Omega, \mathrm{Lf}=200 \mathrm{mH}$ and $\mathrm{Rf}=200 \Omega$. Assume that power supplies have been properly connected to an ideal op-amp and the output voltage is limited to $\pm 10 \mathrm{~V}$


1) (4pt) Find the transfer function $\mathrm{H}(\mathrm{j} \omega)=\operatorname{Vout}(\mathrm{j} \omega) / \mathrm{V} 1(\mathrm{j} \omega)$ for this circuit. (Substitute in the values provided for the components.)
2) ( 2 pt ) What function is this circuit designed to perform at high frequencies $(\mathrm{f} \geq 2 \mathrm{kHz})$ ?
3) (2pt) What function is this circuit designed to perform at low frequencies $(\mathrm{f} \leq 10 \mathrm{~Hz})$ ?
4) ( 4 pt ) What is the corner frequency (in Hz ) for the circuit where it transitions from its low frequency performance to its high frequency performance?
5) (4pt) Sketch the bode plot of $|\mathrm{H}(\mathrm{j} \omega)|, 20 \log$ (magnitude) vs. $\log$ of frequency, of the transfer function from 0.1 to 10 kHz . For simplicity assume that the ideal op-amp output voltage is unlimited.

6) (4pt) For the input below, sketch the output on the same axis. Note the frequency of the input signal.

7) (2pt) For the input below, sketch the output on the same axis. Note the frequency of the input signal.

