Fields and Waves

Lesson 2.4

ELECTROSTATICS - MATERIALS

CONDUCTORS and DIELECTRICS

Conductors

High conductivities; σ (for Copper) ~ 5.8x10⁷ S/m

Dielectrics

Low conductivities; σ (for Rubber) ~ 1x10⁻¹⁵ S/m or 1/ Ω -m

Semiconductors (mid σ 's)

Permittivities, $\varepsilon = 1-100\varepsilon_0$

Note: ε_0 is the permittivity of free space/vacuum = 8.854 x 10⁻¹² F/m

CONDUCTORS

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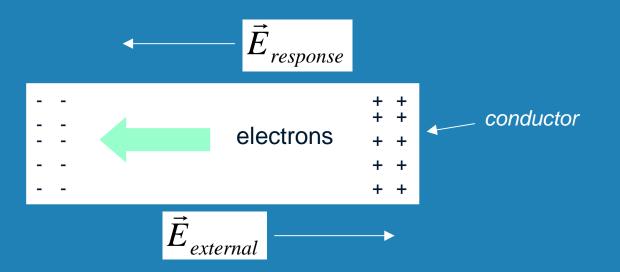
Lattice of Nuclei

Most electrons are stuck to the nucleus

But, 1 or 2 electrons per atom are free to move

This means that if you apply an external E-field, the free electrons will move

CONDUCTORS



Apply external E-field,

- Force on electrons causes free electrons to move
- Charge displacement causes response E-field (opposite to applied external E-field)

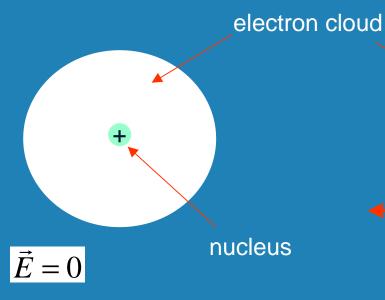
CONDUCTORS

$$ec{E}_{total} = ec{E}_{external} + ec{E}_{response}$$

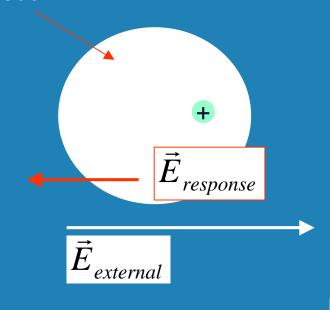
The electrons keep moving until, $ec{E}_{total} = 0$

This means that:

- $ec{E}=0$, in a conductor
- Conductor is equipotential



electron cloud centered on nucleus



Cloud shifts to setup

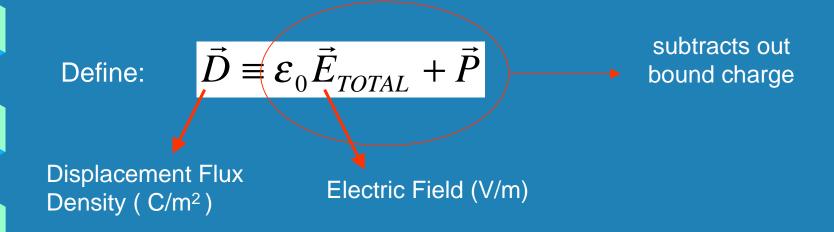
$$ec{E}_{\it response}$$

$$\therefore \vec{E}_{total} = \vec{E}_{external} + \vec{E}_{response} \neq 0$$

Define:
$$\vec{p} = q \cdot d =$$
 dipole moment

$$\vec{E}_{response} \propto -\sum \vec{p}_i = \vec{P}$$
 — Polarization

$$ec{E}_{\it response}$$
 partially cancels applied Field



- $ec{E}_{TOTAL}$ is due to bound/dielectric charge and free charge
- $ec{P}$ is due to bound/dielectric charge only and opposite sign
- $ec{D}$ is due to free charge only

FREE CHARGES

Examples of free charges:

- \rightarrow ρ_s on conductor
- electron beam
- doped region of semi-conductor

Gauss' Law uses just free charge

$$\oint \vec{D} \bullet d\vec{s} = \int \rho \cdot dv = Q_{enclosed}$$

Most general form

Don't need to know about bound charges to find $\hat{m{D}}$

Many materials have $\vec{P} \propto \vec{E}$ $\therefore \vec{D} \propto \vec{E}$

$$\vec{P} \propto \vec{E}$$

$$\vec{L} \cdot \vec{D} \propto \vec{E}$$

Define
$$\vec{D} = \boldsymbol{\varepsilon} \cdot \vec{E}$$
 , where $\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}_r \cdot \boldsymbol{\varepsilon}_0$

$$\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}_r \cdot \boldsymbol{\varepsilon}_0$$

Typically,
$$1 < \varepsilon_r < 10 \rightarrow 100$$

DIELECTRIC BREAKDOWN - part d of problem

Example: Arc in Air

If E-field is too large, it will pull electrons off from atom

These electrons are accelerated by the E-field

These accelerated electrons then collide with more atoms that knock off more electrons



This is an AVALANCHE PROCESS

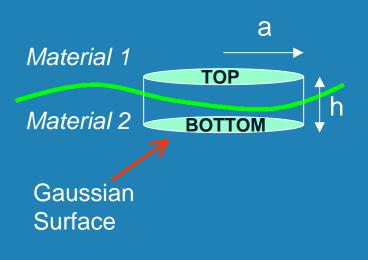
Damages materials - there is a Voltage limit on components, cables in air : $\vec{E}_{breakdown} = 30 \text{ kV/cm}$



BOUNDARY CONDITIONS - Normal Components

all derived from Maxwell's equations

NORMAL COMPONENT



$$\oint \vec{D} \bullet d\vec{s} = Q_{enclosed}$$

Take h << a (a thin disc)

$$Q_{enclosed} = \rho_s \cdot A$$

$$\oint \vec{D} \bullet d\vec{s} = \int_{TOP} \vec{D} \bullet d\vec{s} + \int_{BOTTOM} \vec{D} \bullet d\vec{s}$$

$$= (D_{1n} - D_{2n}) \cdot A$$

$$\therefore D_{1n} - D_{2n} = \rho_s$$

BOUNDARY CONDITIONS - Normal Components

Case 1: REGION 2 is a CONDUCTOR, $D_2 = E_2 = 0$

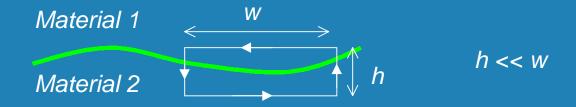
$$\therefore D_{ln} = \rho_s$$

Case 2: REGIONS 1 & 2 are DIELECTRICS with $\rho_s = 0$

$$\therefore D_{1n} = D_{2n}$$

Can only really get ρ_s with conductors

BOUNDARY CONDITIONS - Tangential Components



$$\oint \vec{E} \bullet d\vec{l} = 0 \qquad (E_{2t} - E_{1t}) \cdot w = 0$$

$$\therefore E_{1t} = E_{2t}$$

Note: If region 2 is a conductor $E_{1t} = 0$ Outside conductor E and D are normal to the surface