

Fields and Waves

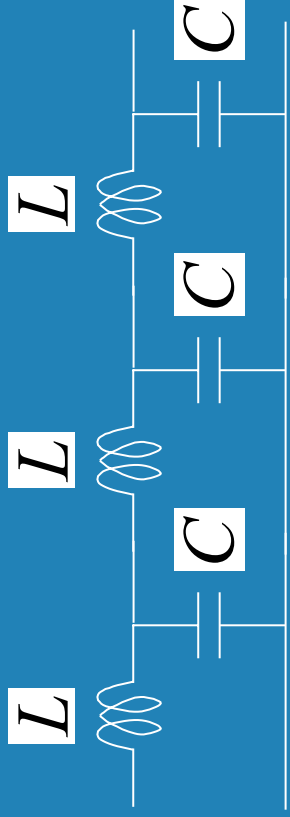
Lesson 4.5

LOSSY TRANSMISSION LINES

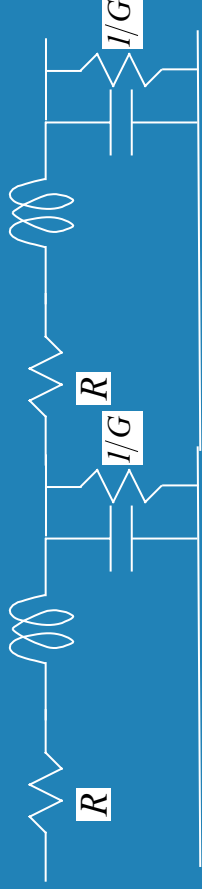
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# Lossless/Lossy Models of TL

Lossless Model of TL:



Lossy Model of TL:



Loss effects due to  
Resistances:

R - resistance of conductors

G - conductivity of insulators

- both are ideally small

# Estimation of R

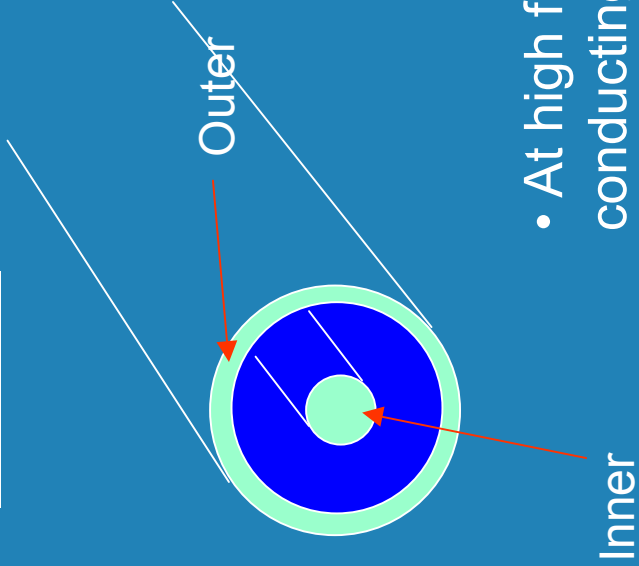
$$R = \frac{l}{\sigma \cdot A}$$

, if constant cross-section

On a per meter basis,

$$r = \frac{l}{\sigma \cdot A_{inner}} + \frac{l}{\sigma \cdot A_{outer}}$$

because inner and outer conductors are in series

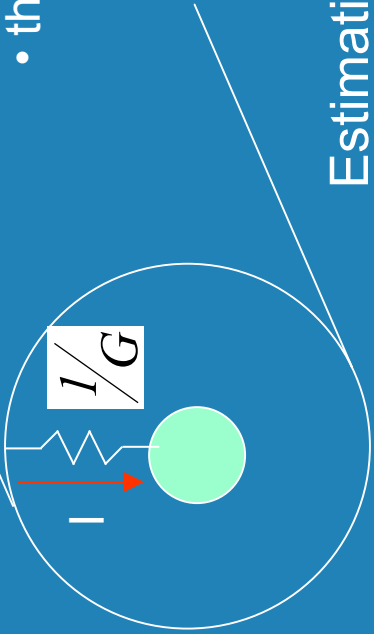


- At high frequencies, not all the copper is used for conducting (see Lesson 3.1)
- Current only flows in outer portion due to skin depth effects

# Estimation of G

The  $1/G$  component represents radial current flow, due to small  $\sigma$  of insulator

- the cross-sectional area is not constant



$$\therefore G = \frac{l}{R} \neq \frac{\sigma \cdot A}{l}$$

$$G = \frac{l}{R} = \frac{l}{V} = \frac{\int \vec{j} \cdot d\vec{s}}{V_{ab}}$$

$$= \frac{\sigma}{\epsilon} \cdot \frac{\int \vec{D} \cdot d\vec{s}}{V_{ab}} = \frac{\sigma}{\epsilon} \cdot \frac{Q}{V_{ab}} = \frac{\sigma}{\epsilon} \cdot C$$

Estimation of G:



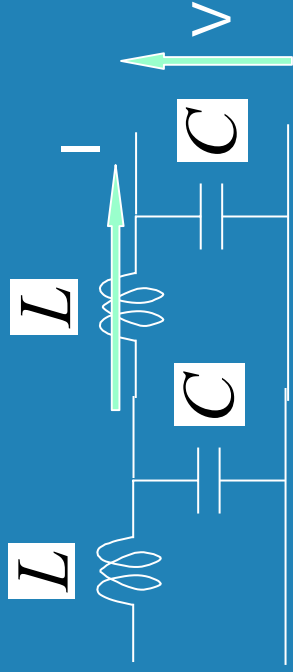
From Electrostatics,

$$\vec{j} = \sigma \cdot \vec{E} = \frac{\sigma}{\epsilon} \cdot \vec{D}$$

Also,  $g = \frac{G}{l} = \frac{\sigma}{\epsilon} \cdot c$

Do Problem 1a & 1b

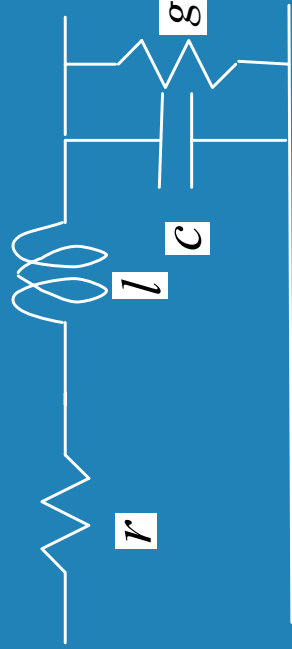
# Effects on $Z_c$ - Characteristic Impedance



For Lossless system,  
 $R_c$  represents

$$\hat{V} = \hat{I}$$

$$R_c = \sqrt{\frac{L}{C}}$$



Replace  $j \cdot \omega \cdot l$  with  $r + j \cdot \omega \cdot l$

Replace  $j \cdot \omega \cdot c$  with  $g + j \cdot \omega \cdot c$

Characteristic  
Impedance

$$Z_c = \sqrt{\frac{r + j \cdot \omega \cdot l}{g + j \cdot \omega \cdot c}}$$

# Attenuation Factor

For lossless systems:

$$\beta = \omega \cdot \sqrt{l \cdot c}$$

For lossy systems:

$$\gamma = \alpha + j \cdot \beta = \sqrt{(r + j \cdot \omega \cdot l)(g + j \cdot \omega \cdot c)}$$

The phasors have the factor:

$$e^{-\gamma \cdot z} = e^{-\alpha \cdot z} \cdot e^{-j \cdot \beta \cdot z}$$

Attenuation/loss factor due to resistance