

Electromagnetic Plane Waves in Lossless Media

Reading assignment

Ulaby, 7-1, 7-2, 7-6.1

Connor and Salon, Unit IX

Problem 1 - Intro to electromagnetic waves

The electric field of a plane wave is given by $\mathbf{E} = E_m \cos(\omega t - \beta z) \mathbf{a}_x$.

- Write \mathbf{E} in phasor form.
- Under what conditions does \mathbf{E} satisfy the wave equation (in phasor form), $\partial^2 E_x / \partial z^2 = -\mu\epsilon\omega^2 E_x$?
- What is the velocity of a plane wave in free space?
- What are typical values of f , ω , T ($=1/f$), β , and λ for X-rays, visible light, microwaves, and FM radio in free space? (Check the walls of the studio).
- Find \mathbf{H} using the phasor form of the $\nabla \times \mathbf{E}$ equation. Assume the \mathbf{E} and \mathbf{H} phasors are only a function of z .
- Evaluate the amplitude ratio, $\eta = |\mathbf{E}| / |\mathbf{H}|$. Express η in terms of material properties.
- If \mathbf{E} was in the \mathbf{a}_y direction, what direction would \mathbf{H} be in?
- Run the Java applet linked through the course homepage.
- How many independent parameters are there in the following set?
 $\omega, \beta, \mu, \epsilon, \eta, \lambda, T$

Problem 2 - Waves in lossless media

WRPI broadcasts at 91.5 MHz. The amplitude of \mathbf{E} on campus is roughly 0.08 V/m. Assume a coordinate system in which the wave is polarized in the \mathbf{a}_y direction and propagating in the \mathbf{a}_z direction. Assume the phase = 0 at $z = 0$.

- What are β , η and λ for this wave?
- Write the electric and magnetic fields in phasor form.
- Write the electric field in time domain form.

Problem 3 - Energy & Power - lossless media

- What is the average energy density of the electric and magnetic fields for the WRPI signal on campus? (Use Prob. 2 results).
- What is the time average Poynting vector of the wave, \mathbf{S}_{av} ? Divide its magnitude by the speed of light and compare with your answer from part a.
- The transmitter is about 10 km from campus. What transmitter power is required to radiate the same power density into a sphere of radius 10 km?